

1. A block of mass  $m$  slides on a frictionless inclined plane which is driven so that it moves horizontally. The displacement of the plane at time  $t$  is some function  $x(t)$ . Use d'Alembert's principle to find the equation of motion of the block taking the displacement  $s$  of the block down the plane as the generalized coordinate.

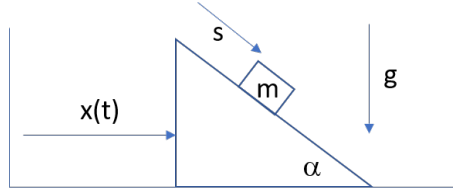


Figure 1:

2. A mass  $m$  is attached to a light cord which wraps around a frictionless pulley of mass  $M$ , radius  $R$ , and moment of inertial  $I$ . Gravity  $g$  acts vertically downwards. Use d'Alembert's principle to find the acceleration of  $m$ .
3. Masses  $m$  and  $2m$  are connected by a light inextensible string which passes over a pulley of mass  $2m$  and radius  $a$ . Write the Lagrangian and find the acceleration of the system.
4. The point of support of a simple pendulum of mass  $M$  and length  $L$  is moving along horizontal axis with a constant velocity  $V$ . Write down the Lagrange equation.
5. A simple pendulum that is free to swing the entire solid angle is called a spherical pendulum. Find the differential equation of motion of a spherical pendulum using Lagrange's method. Also show that the angular momentum about a vertical axis through the point of support is a constant of motion.
6. Consider a bead of mass  $m$  sliding without friction on a wire bent in the shape of a parabola, which is spun with a constant angular velocity  $\omega$  about its vertical axis. Use cylindrical polar coordinates and let the equation of the parabola be  $z = k\rho^2$ . Write down the Lagrangian in terms of  $\rho$  as the generalised coordinate. Find the equation of motion of the bead and determine whether there are positions of equilibrium (i.e. there are value of  $\rho$  at which the bead can remain fixed without sliding up or down the spinning wire).

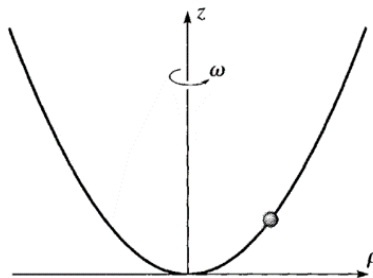


Figure 2: